

Compiling Dynamic Information Flow Control

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NJPLS Fall 2012



DIFC

```
let y = secret + x
```

```
let z = if secret then true else false
```

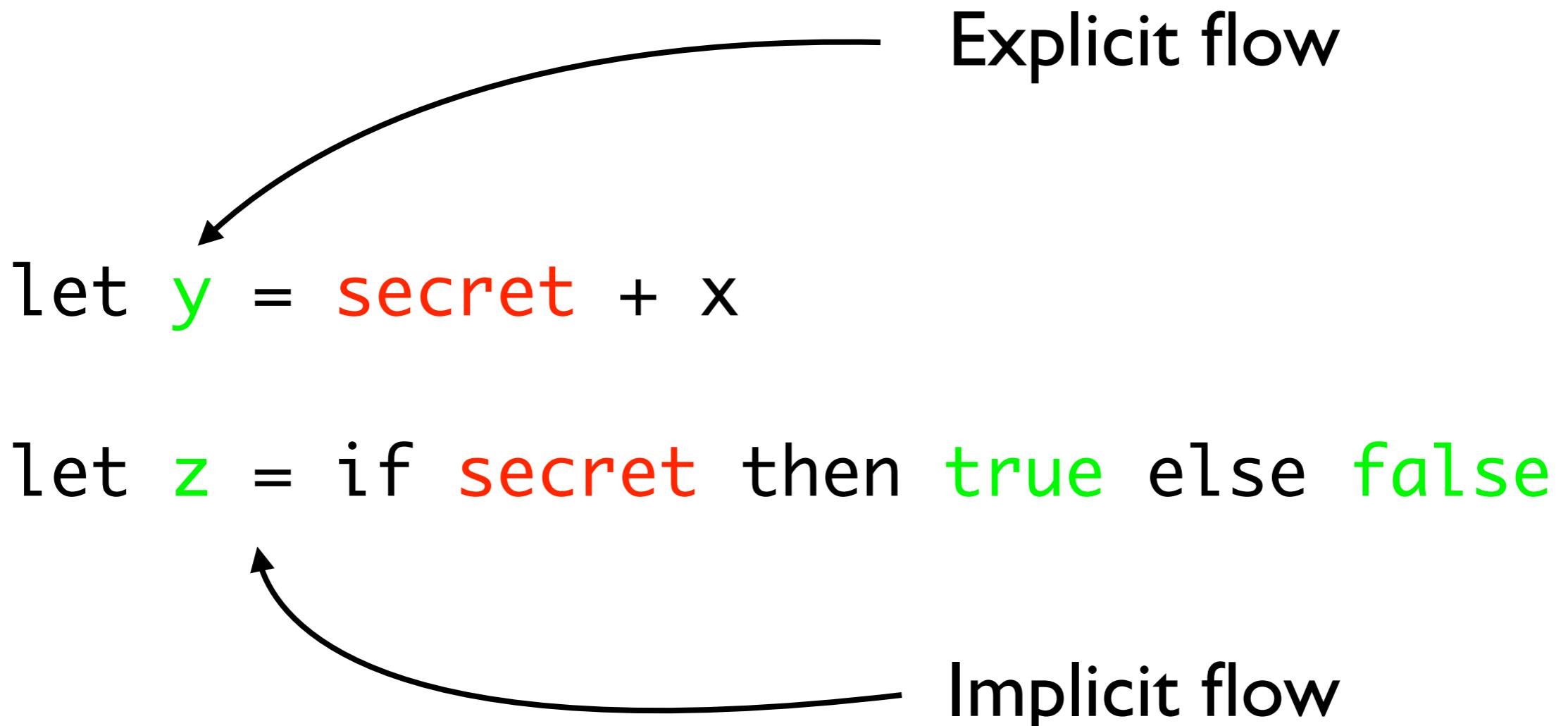
DIFC

Explicit flow

let `y = secret + x`

let `z = if secret then true else false`

DIFC



Label lattices

Let $(L, \sqsubseteq, \sqcup, \perp, \top)$ be a **bounded lattice**

Operations **join** their arguments

$$\text{pc}, 5@l + 6@h \rightarrow \text{pc}, 11@h$$

Labels go on **values** and on the **program counter** (**pc**)

$$\text{pc}, \text{if true}@h \text{ then } 1 \text{ else } 0 \rightarrow \text{pc} \sqcup h, 1$$

Not-a-Value values (NaVs)

- Catalin's talk?

Not-a-Value values (NaVs)

- Fine-grained **DIFC** \Rightarrow **delayed exceptions**
- NaVs are **first-class** and **labeled**
- NaVs propagate via **dataflow**

$3 + (5/0) \Rightarrow \text{NaV}(\text{"divide by zero"})$

$(4,2).3 + (5/0) \Rightarrow \text{NaV}(\text{"out of bounds"})$

Compiling DIFC

- What's labeled?
- Where are labels kept?
- Interoperability
 - With labeled programs
 - With unlabeled programs

The SAFE ISA: A DIFC Architecture

- Every word of memory labeled
- Richly configurable tagged architecture
 - OS support for DIFC
- No escape hatch
- No direct interoperation with unlabeled code

Compiling DIFC on Stock Hardware

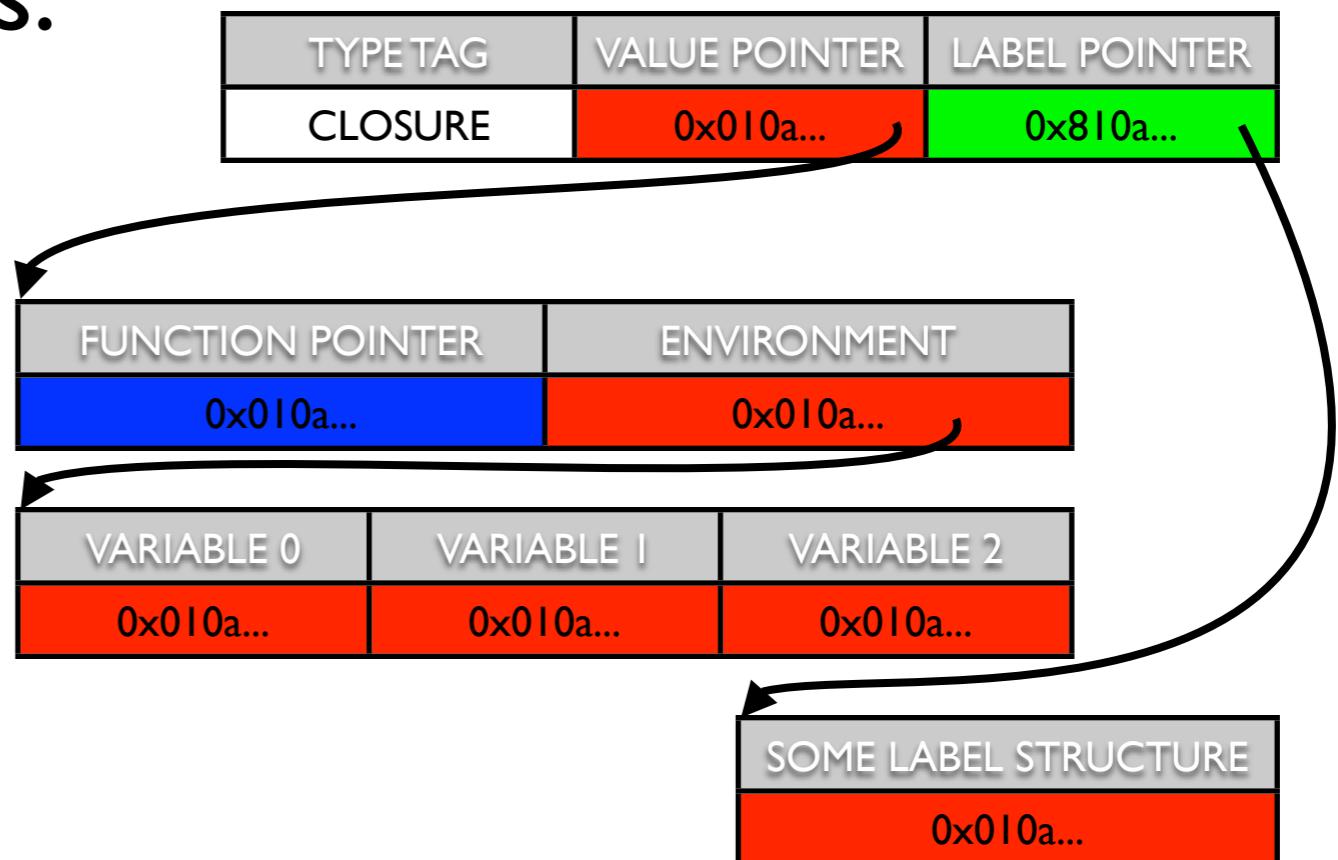
- IFC rules are an **abstraction**
 - Implementation can vary
 - **Observably** play by the rules
 - Do what you like when **nobody's looking!**

What am I doing?

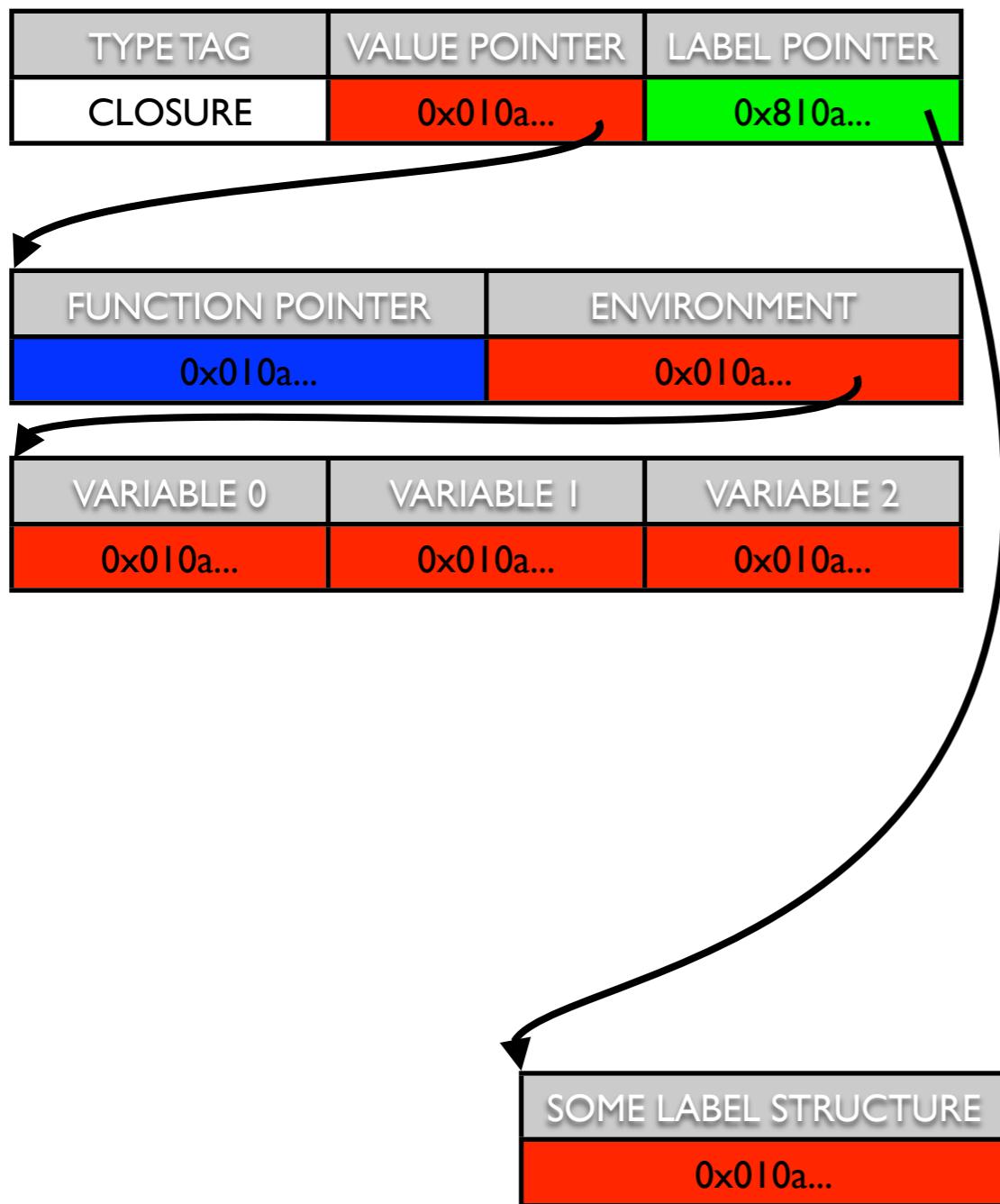
- Compiling a **simple DIFC language** on x86
 - Pure functional, **non-interfering** variant of **Breeze**
 - **LLVM** back-end

What's labeled?

- Language **values** are labeled
 - Stored **in-line**, with the type tag
- Unlabeled things:
 - Closures
 - Environment
 - Tuple arrays

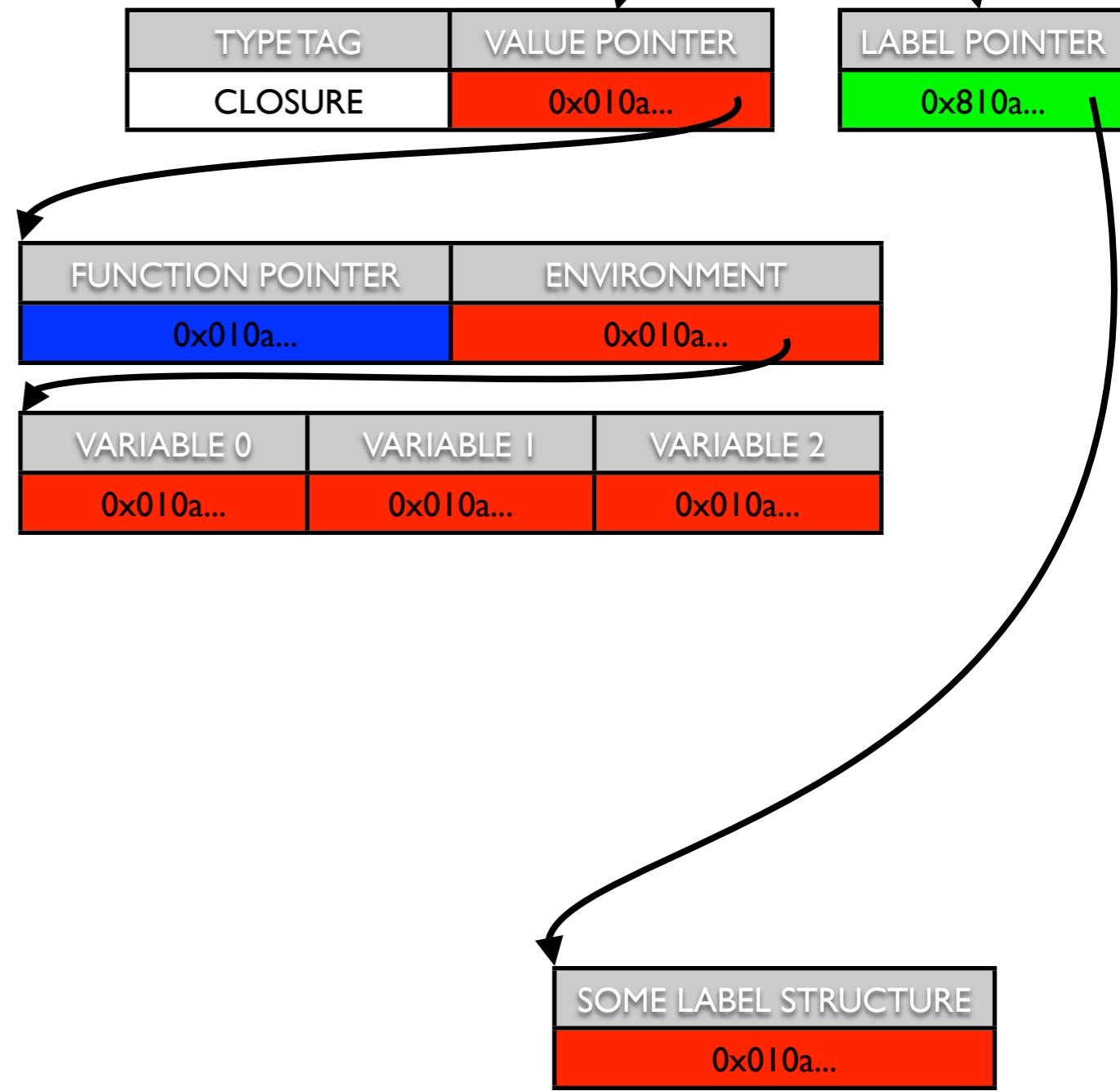


Inline tags



Shadow space

Hash? Address + constant?



Let's compute $x + y$

```

let $x116 = 128@i8;
let $x117 = $x116 == $x108;
let ($pc142,$x141) =
  if $x117
    then ($x97,$x69)
  else let $x119 = $x51 == $x108;
    let ($pc140,$x139) =
      if $x119
        then let $x121 = $x116 == $x112;
          let ($pc134,$x133) =
            if $x121
              then ($x97,$x98)
            else let $x123 = $x51 == $x112;
              let ($pc132,$x131) =
                if $x123
                  then let $x124 = $x109 + $x113;
                    let $x126 = ($x51,$x124,$x115)@heap;
                      ($x97,$x126)
                    else let $x127 = "type error, expected int";
                      let $x128 = cast $x127 : [i8]@heap to i64;
                      let $x130 = ($x116,$x128,$x115)@heap;
                        ($x97,$x130) : ptr(<i8,i64,i64>@heap);
                      ($pc132,$x131) : ptr(<i8,i64,i64>@heap);
                    ($pc134,$x133)
                  else let $x135 = "type error, expected int";
                    let $x136 = cast $x135 : [i8]@heap to i64;
                    let $x138 = ($x116,$x136,$x110)@heap;
                      ($x97,$x138) : ptr(<i8,i64,i64>@heap);
                    ($pc140,$x139) : ptr(<i8,i64,i64>@heap);
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```

Let's compute $x + y$

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```

Type checks

Let's compute $x + y$

```

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```

NaV checks

Type checks

Let's compute $x + y$

```

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        then let $x121 = $x116 == $x112;
          let ($pc134,$x133) =
            if $x121 ←
              then ($x97,$x98)
            else let $x123 = $x51 == $x112;
              let ($pc132,$x131) =
                if $x123 ←
                  then let $x124 = $x109 + $x113; ←
                    let $x126 = ($x51,$x124,$x115)@heap;
                      ($x97,$x126)
                    else let $x127 = "type error, expected int";
                      let $x128 = cast $x127 : [i8]@heap to i64;
                      let $x130 = ($x116,$x128,$x115)@heap;
                        ($x97,$x130) : ptr(<i8,i64,i64>@heap);
                      ($pc132,$x131) : ptr(<i8,i64,i64>@heap);
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                  ($pc142,$x141)

```

NaV checks

Type checks

Actual operation!

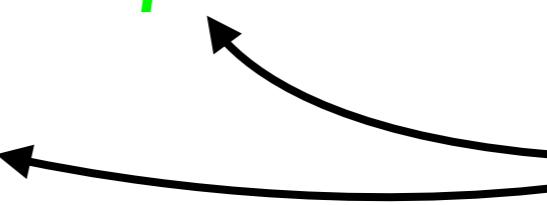
Let's compute $x + y$

Optimization

Low level strategies

- Sound implementations of IFC abstractions
- Optimize!
 - Typed ANF IR that explicitly unpacks labels
 - LLVM backend
- Exploit NaVs

High level strategies

- Label lattice properties are optimizations
 - \perp is the identity for \sqcup
 - \sqcup is idempotent; \sqsubseteq is reflexive
- *Abstract interpretation in the label lattice*
- *Contracts*  Work in progress!

Optimizations in action

$f = \lambda x. (x * x) + 5;$

```
fun $clo0 (x,$env,$pc) =
let $x0 = load x;
let $x1 = $x0.0;
let $x2 = $x0.1;
let $x3 = $x0.2;
let $x4 = load x;
let $x5 = $x4.0;
let $x6 = $x4.1;
let $x7 = $x4.2;
let $x8 = $x3 ∨ $x7;
let $x9 = 2@i8;
let $x10 = $x9 == $x1;
let ($pc27,$x26) =
if $x10
then let $x11 = 2@i8;
let $x12 = $x11 == $x5;
let ($pc21,$x20) = if $x12 then let $x13 = $x2 * $x6;
let $x14 = 2@i8;
let $x15 = ($x14,$x13,$x8)@heap;
($pc,$x15) else let $x16 = "type error, expected int";
let $x17 = cast $x16 : [i8]@heap to i64;
let $x18 = 128@i8;
let $x19 = ($x18,$x17,$x8)@heap;
($pc,$x19) : ptr(<i8,i64,i64>@heap);
($pc21,$x20) else let $x22 = "type error, expected int";
let $x23 = cast $x22 : [i8]@heap to i64;
let $x24 = 128@i8;
let $x25 = ($x24,$x23,$x3)@heap;
($pc,$x25) : ptr(<i8,i64,i64>@heap);

let $anf0 = $x26;
let $x28 = 5@i64;
let $x29 = bottom;
let $x30 = 2@i8;
let $x31 = ($x30,$x28,$x29)@heap;
let $anf1 = $x31;
let $x32 = load $anf0;
let $x33 = $x32.0;
let $x34 = $x32.1;
let $x35 = $x32.2;
let $x36 = load $anf1;
let $x37 = $x36.0;
let $x38 = $x36.1;
let $x39 = $x36.2;
let $x40 = $x35 ∨ $x39;
let $x41 = 2@i8;
let $x42 = $x41 == $x33;
let ($pc59,$x58) =
if $x42
then let $x43 = 2@i8;
let $x44 = $x43 == $x37;
let ($pc53,$x52) = if $x44
then let $x45 = $x34 + $x38;
let $x46 = 2@i8;
let $x47 = ($x46,$x45,$x40)@heap;
($pc27,$x47)
else let $x48 = "type error, expected int";
let $x49 = cast $x48 : [i8]@heap to i64;
let $x50 = 128@i8;
let $x51 = ($x50,$x49,$x40)@heap;
($pc27,$x51) : ptr(<i8,i64,i64>@heap);
($pc53,$x52)
else let $x54 = "type error, expected int";
let $x55 = cast $x54 : [i8]@heap to i64;
let $x56 = 128@i8;
let $x57 = ($x56,$x55,$x35)@heap;
($pc27,$x57) : ptr(<i8,i64,i64>@heap);
let $anf2 = $x58;
($pc59,$anf2);
```

Optimizations in action

Unoptimized

```
fun $clo0 (x,$env,$pc) =
  let $x0 = load x;
  let $x1 = $x0.0;
  let $x2 = $x0.1;
  let $x3 = $x0.2;
  let $x4 = load x;
  let $x5 = $x4.0;
  let $x6 = $x4.1;
  let $x7 = $x4.2;
  let $x8 = $x3 ∪ $x7;
  let $x9 = 2@i8;
  let $x10 = $x9 == $x1;
  let ($pc27,$x26) =
    if $x10
    then let $x11 = 2@i8;
         let $x12 = $x11 == $x5;
         let ($pc21,$x20) = if $x12 then let $x13 = $x2 * $x6;
                                         let $x14 = 2@i8;
                                         let $x15 = ($x14,$x13,$x8)@heap;
                                         ($pc,$x15) else let $x16 = "type error, expected int";
                                                       let $x17 = cast $x16 : [i8]@heap to i64;
                                                       let $x18 = 128@i8;
                                                       let $x19 = ($x18,$x17,$x8)@heap;
                                                       ($pc,$x19) : ptr(<i8,i64,i64>@heap);
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                                                       let $x25 = ($x24,$x23,$x3)@heap;
                                                       ($pc,$x25) : ptr(<i8,i64,i64>@heap);
                                         ($pc21,$x20)
    let $anf0 = $x26;
    let $x28 = 5@i64;
    let $x29 = bottom;
    let $x30 = 2@i8;
    let $x31 = ($x30,$x28,$x29)@heap;
    let $anf1 = $x31;
    let $x32 = load $anf0;
    let $x33 = $x32.0;
    let $x34 = $x32.1;
    let $x35 = $x32.2;
    let $x36 = load $anf1;
    let $x37 = $x36.0;
    let $x38 = $x36.1;
    let $x39 = $x36.2;
    let $x40 = $x35 ∪ $x39;
    let $x41 = 2@i8;
    let $x42 = $x41 == $x33;
    let ($pc59,$x58) =
      if $x42
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           let ($pc53,$x52) = if $x44
             then let $x45 = $x34 + $x38;
                  let $x46 = 2@i8;
                  let $x47 = ($x46,$x45,$x40)@heap;
                  ($pc27,$x47)
             else let $x48 = "type error, expected int";
                  let $x49 = cast $x48 : [i8]@heap to i64;
                  let $x50 = 128@i8;
                  let $x51 = ($x50,$x49,$x40)@heap;
                  ($pc27,$x51) : ptr(<i8,i64,i64>@heap);
                  ($pc53,$x52)
           else let $x54 = "type error, expected int";
                let $x55 = cast $x54 : [i8]@heap to i64;
                let $x56 = 128@i8;
                let $x57 = ($x56,$x55,$x35)@heap;
                ($pc27,$x57) : ptr(<i8,i64,i64>@heap);
                ($pc53,$x52)
      let $anf2 = $x58;
      ($pc59,$anf2);
```

Optimized

```
fun $clo0 (x,$env,$pc) =
  let $x0 = load x;
  let $x1 = $x0.0;
  let $x2 = $x0.1;
  let $x3 = $x0.2;
  let $x9 = 2@i8;
  let $x10 = $x9 == $x1;
  let ($pc27,$x26) =
    if $x10
    then let $x13 = $x2 * $x2;
         let $x15 = ($x9,$x13,$x3)@heap;
         ($pc,$x15)
    else let $x22 = "type error, expected int";
         let $x23 = cast $x22 : [i8]@heap to i64;
         let $x24 = 128@i8;
         let $x25 = ($x24,$x23,$x3)@heap;
         ($pc,$x25) : ptr(<i8,i64,i64>@heap);
  let $x32 = load $x26;
  let $x33 = $x32.0;
  let $x34 = $x32.1;
  let $x35 = $x32.2;
  let $x38 = 5@i64;
  let $x42 = $x9 == $x33;
  let ($pc59,$x58) =
    if $x42
    then let $x45 = $x34 + $x38;
         let $x47 = ($x9,$x45,$x35)@heap;
         ($pc27,$x47)
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         let $x56 = 128@i8;
         let $x57 = ($x56,$x55,$x35)@heap;
         ($pc27,$x57) : ptr(<i8,i64,i64>@heap);
         ($pc59,$x58);
```

Optimizations in action

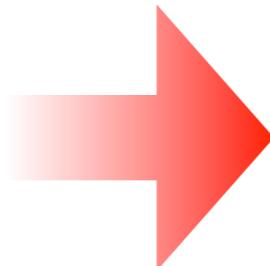
Unoptimized Optimized
Joins eliminated!

```
fun $clo0 (x,$env,$pc) =  
let $x0 = load x;  
let $x1 = $x0.0;  
let $x2 = $x0.1;  
let $x3 = $x0.2;  
let $x4 = load x;  
let $x5 = $x4.0;  
let $x6 = $x4.1;  
let $x7 = $x4.2;  
let $x8 = $x3 ∪ $x7;  
let $x9 = 2@i8;  
let $x10 = $x9 == $x1;  
let ($pc27,$x26) =  
if $x10  
then let $x11 = 2@i8;  
let $x12 = $x11 == $x5;  
let ($pc21,$x20) = if $x12 then let $x13 = $x2 * $x6;  
let $x14 = 2@i8;  
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($pc,$x25) : ptr(<i8,i64,i64>@heap);  
  
let $anf0 = $x26;  
let $x28 = 5@i64;  
let $x29 = bottom;  
let $x30 = 2@i8;  
let $x31 = ($x30,$x28,$x29)@heap;  
let $anf1 = $x31;  
let $x32 = load $anf0;  
let $x33 = $x32.0;  
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let $x51 = ($x50,$x49,$x40)@heap;  
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($pc53,$x52)  
else let $x54 = "type error, expected int";  
let $x55 = cast $x54 : [i8]@heap to i64;  
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```
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then let $x13 = $x2 * $x2;  
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```

CSE

```
fun $clo0 (x,$env,$pc) =  
  let $x0 = load x;  
    let $x1 = $x0.0;  
    let $x2 = $x0.1;  
    let $x3 = $x0.2;  
    let $x4 = load x;  
    let $x5 = $x4.0;  
    let $x6 = $x4.1;  
    let $x7 = $x4.2;  
  let $x8 = $x3 ∙ $x7;  
  ...
```

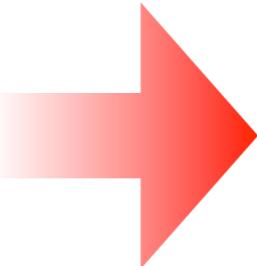


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  let $x0 = load x;  
    let $x1 = $x0.0;  
    let $x2 = $x0.1;  
    let $x3 = $x0.2;  
    let $x8 = $x3 ∙ $x3;  
  ...
```

$f = \lambda x. (x * x) + 5;$

Reflexivity

```
fun $clo0 (x,$env,$pc) =  
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    let $x1 = $x0.0;  
    let $x2 = $x0.1;  
    let $x3 = $x0.2;  
    let $x8 = $x3 □ $x3;  
    ...
```

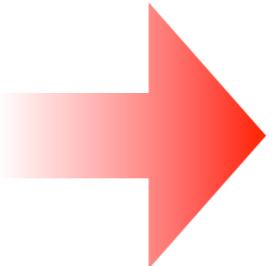


```
fun $clo0 (x,$env,$pc) =  
    let $x0 = load x;  
    let $x1 = $x0.0;  
    let $x2 = $x0.1;  
    let $x3 = $x0.2;  
    let $x8 = $x3;  
    ...
```

$f = \lambda x. (x * x) + 5;$

Variable reduction

```
fun $clo0 (x,$env,$pc) =  
    let $x0 = load x;  
    let $x1 = $x0.0;  
    let $x2 = $x0.1;  
    let $x3 = $x0.2;  
    let $x8 = $x3;  
    ...
```



```
fun $clo0 (x,$env,$pc) =  
    let $x0 = load x;  
    let $x1 = $x0.0;  
    let $x2 = $x0.1;  
    let $x3 = $x0.2;  
    ...[$x8 ↪ $x3]
```

$f = \lambda x. (x * x) + 5;$

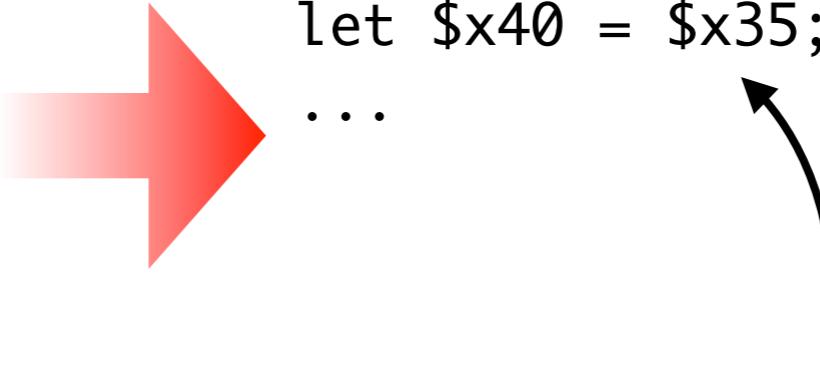
Constant folding

```
...
let $anf0 = $x26;
let $x28 = 5@i64;
let $x29 = bottom;
let $x30 = 2@i8;
let $x31 = ($x30,$x28,$x29)@heap;
let $anf1 = $x31;
let $x32 = load $anf0;
let $x33 = $x32.0;
let $x34 = $x32.1;
let $x35 = $x32.2;
let $x36 = load $anf1;
let $x37 = $x36.0;
let $x38 = $x36.1;
let $x39 = $x36.2;
let $x40 = $x35 □ $x39;
...
```

$$f = \lambda x. (x * x) + 5;$$

Constant folding

```
...  
let $anf0 = $x26;  
let $x28 = 5@i64;  
let $x29 = bottom;  
let $x30 = 2@i8;  
let $x31 = ($x30,$x28,$x29)@heap;  
let $anf1 = $x31;  
let $x32 = load $anf0;  
let $x33 = $x32.0;  
let $x34 = $x32.1;  
let $x35 = $x32.2;  
let $x36 = load $anf1;  
let $x37 = $x36.0;  
let $x38 = $x36.1;  
let $x39 = $x36.2;  
let $x40 = $x35 ⊔ $x39;  
...
```



```
...  
let $x32 = load $x26;  
let $x33 = $x32.0;  
let $x34 = $x32.1;  
let $x35 = $x32.2;  
let $x38 = 5@i64;  
let $x40 = $x35;  
...
```

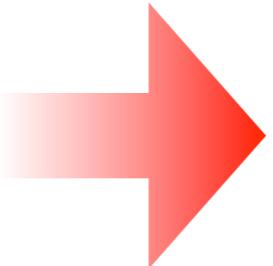
Bottom is a lattice identity

```
let $x40 = $x35 ⊔ bottom;
```

$f = \lambda x. (x * x) + 5;$

Variable reduction

```
...  
let $x32 = load $x26;  
let $x33 = $x32.0;  
let $x34 = $x32.1;  
let $x35 = $x32.2;  
let $x38 = 5@i64;  
let $x40 = $x35;  
...
```



```
...  
let $x32 = load $x26;  
let $x33 = $x32.0;  
let $x34 = $x32.1;  
let $x35 = $x32.2;  
let $x38 = 5@i64;  
...[$40 ↦ $x35]
```

$f = \lambda x. (x * x) + 5;$

Lattice operations in the IR

- Most **IR constructs** correspond to **LLVM**
- EBottom, EJoin, EFlowsTo AST nodes **don't**
 - **Abstract** representation
 - Enables **optimizations**
 - Constant folding has a **VBottom**

Stupid NaV tricks

- Dedicated “is a NaV” bit in type tags
- For **safe** operations on values:
 - Perform the operation **regardless**
 - **Bitwise AND** the tags
 - Check the **NaV** bit
 - Error info stored on the side (DWARF)

NaV branch minimization*

```
let $x116 = 128@i8;
let $x117 = $x116 == $x108;
let ($pc142,$x141) =
  if $x117
    then ($x97,$x69)
  else let $x119 = $x51 == $x108;
    let ($pc140,$x139) =
      if $x119
        then let $x121 = $x116 == $x112;
          let ($pc134,$x133) =
            if $x121
              then ($x97,$x98)
            else let $x123 = $x51 == $x112;
              let ($pc132,$x131) =
                if $x123
                  then let $x124 = $x109 + $x113;
                    let $x126 = ($x51,$x124,$x115)@heap;
                      ($x97,$x126)
                    else let $x127 = "type error, expected int";
                      let $x128 = cast $x127 : [i8]@heap to i64;
                      let $x130 = ($x116,$x128,$x115)@heap;
                        ($x97,$x130) : ptr(<i8,i64,i64>@heap);
                      ($pc132,$x131) : ptr(<i8,i64,i64>@heap);
                    ($pc134,$x133)
                  else let $x135 = "type error, expected int";
                    let $x136 = cast $x135 : [i8]@heap to i64;
                    let $x138 = ($x116,$x136,$x110)@heap;
                      ($x97,$x138) : ptr(<i8,i64,i64>@heap);
                    ($pc140,$x139) : ptr(<i8,i64,i64>@heap);
                  ($pc142,$x141)
```

Computing $x + y$

* *Work in progress*

NaV branch minimization*

```
let $x116 = 128@i8;
let $x117 = $x116 == $x108;
let ($pc142,$x141) =
  if $x117
    then ($x97,$x69)
  else let $x119 = $x51 == $x108;
    let ($pc140,$x139) =
      if $x119 ←
        then let $x121 = $x116 == $x112;
          let ($pc134,$x133) =
            if $x121
              then ($x97,$x98)
            else let $x123 = $x51 == $x112;
              let ($pc132,$x131) =
                if $x123 ←
                  then let $x124 = $x109 + $x113;
                    let $x126 = ($x51,$x124,$x115)@heap;
                      ($x97,$x126)
                    else let $x127 = "type error, expected int";
                      let $x128 = cast $x127 : [i8]@heap to i64;
                      let $x130 = ($x116,$x128,$x115)@heap;
                        ($x97,$x130) : ptr(<i8,i64,i64>@heap);
                      ($pc132,$x131) : ptr(<i8,i64,i64>@heap);
                    ($pc134,$x133)
                  else let $x135 = "type error, expected int";
                    let $x136 = cast $x135 : [i8]@heap to i64;
                    let $x138 = ($x116,$x136,$x110)@heap;
                      ($x97,$x138) : ptr(<i8,i64,i64>@heap);
                    ($pc140,$x139) : ptr(<i8,i64,i64>@heap);
                  ($pc142,$x141)
```

Type checks

Computing $x + y$

* Work in progress

NaV branch minimization*

```
let $x116 = 128@i8;
let $x117 = $x116 == $x108;
let ($pc142,$x141) =
  if $x117 ←
    then ($x97,$x69)
    else let $x119 = $x51 == $x108;
         let ($pc140,$x139) =
           if $x119 ←
             then let $x121 = $x116 == $x112;
                  let ($pc134,$x133) =
                    if $x121 ←
                      then ($x97,$x98)
                      else let $x123 = $x51 == $x112;
                           let ($pc132,$x131) =
                             if $x123 ←
                               then let $x124 = $x109 + $x113;
                                    let $x126 = ($x51,$x124,$x115)@heap;
                                    ($x97,$x126)
                                    else let $x127 = "type error, expected int";
                                         let $x128 = cast $x127 : [i8]@heap to i64;
                                         let $x130 = ($x116,$x128,$x115)@heap;
                                         ($x97,$x130) : ptr(<i8,i64,i64>@heap);
                                         ($pc132,$x131) : ptr(<i8,i64,i64>@heap);
                                         ($pc134,$x133)
                                         else let $x135 = "type error, expected int";
                                              let $x136 = cast $x135 : [i8]@heap to i64;
                                              let $x138 = ($x116,$x136,$x110)@heap;
                                              ($x97,$x138) : ptr(<i8,i64,i64>@heap);
                                              ($pc140,$x139) : ptr(<i8,i64,i64>@heap);
                                              ($pc142,$x141)
```

NaV checks

Type checks

Computing $x + y$

* Work in progress

NaV branch minimization*

```
let $x116 = 128@i8;
let $x117 = $x116 == $x108;
let ($pc142,$x141) =
  if $x117 ←
    then ($x97,$x69)
  else let $x119 = $x51 == $x108;
    let ($pc140,$x139) =
      if $x119 ←
        then let $x121 = $x116 == $x112;
          let ($pc134,$x133) =
            if $x121 ←
              then ($x97,$x98)
            else let $x123 = $x51 == $x112;
              let ($pc132,$x131) =
                if $x123 ←
                  then let $x124 = $x109 + $x113; ←
                      let $x126 = ($x51,$x124,$x115)@heap;
                      ($x97,$x126)
                    else let $x127 = "type error, expected int";
                      let $x128 = cast $x127 : [i8]@heap to i64;
                      let $x130 = ($x116,$x128,$x115)@heap;
                      ($x97,$x130) : ptr(<i8,i64,i64>@heap);
                    ($pc132,$x131) : ptr(<i8,i64,i64>@heap);
                  ($pc134,$x133)
                else let $x135 = "type error, expected int";
                  let $x136 = cast $x135 : [i8]@heap to i64;
                  let $x138 = ($x116,$x136,$x110)@heap;
                  ($x97,$x138) : ptr(<i8,i64,i64>@heap);
                ($pc140,$x139) : ptr(<i8,i64,i64>@heap);
              ($pc142,$x141)
```

NaV checks

Type checks

Actual operation!

Computing $x + y$

* Work in progress

NaV branch minimization*

```
let $x116 = 128@i8;
let $x117 = $x116 == $x108;
let ($pc142,$x141) =
  if $x117 ←
    then ($x97,$x69)
  else let $x119 = $x51 == $x108;
    let ($pc140,$x139) =
      if $x119 ←
        then let $x121 = $x116 == $x112;
          let ($pc134,$x133) =
            if $x121 ←
              then ($x97,$x98)
            else let $x123 = $x51 == $x112;
              let ($pc132,$x131) :
                if $x123 ←
                  then let $x124 = $x109 + $x113; ←
                    let $x126 = ($x51,$x124,$x115)@heap;
                      ($x97,$x126)
                    else let $x127 = "type error, expected int";
                      let $x128 = cast $x127 : [i8]@heap to i64;
                      let $x130 = ($x116,$x128,$x115)@heap;
                        ($x97,$x130) : ptr(<i8,i64,i64>@heap);
                      ($pc132,$x131) : ptr(<i8,i64,i64>@heap);
                    ($pc134,$x133)
                  else let $x135 = "type error, expected int";
                    let $x136 = cast $x135 : [i8]@heap to i64;
                    let $x138 = ($x116,$x136,$x110)@heap;
                      ($x97,$x138) : ptr(<i8,i64,i64>@heap);
                    ($pc140,$x139) : ptr(<i8,i64,i64>@heap);
                  ($pc142,$x141)
```

NaV checks

Type checks

Actual operation!

Computing $x + y$

* Work in progress

NaV branch minimization

Single branch in non-NaV case

```
let $x51 = 2@i8; // int tag
...
let $x124 = $x109 + $x113;
let $fstok = $x108 == $x51;
let $sndok = $x112 == $x51;
let $bothok = $fstok && $sndok;
let ($pc142,$x141) =
    if $bothok
        then let $x126 = ($x51,$x124,$x115)@heap;
              ($x97,$x126)
        else ... // check tags, figure out which NaV to return
```

Computing $\mathbf{x} + \mathbf{y}$

NaV branch minimization

```
let $x116 = 128@i8; // nav tag
let $navbits = $x108 | $x112;
let $havenav = $x116 & $navbits;
let ($pc142,$x141) =
  if $havenav
    then ... choose between ($x97,$x69) and ($x97,$x98) ...
  else ... // some parametric operation
```

NaV-strict,
parametric
operations

Outlook

- Finishing up compiler now
- Lots of **evaluation** to do
- Beyond performance: **questions!**
 - Interoperability
 - Contracts